



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

## **NATIONAL SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P2**

**NOVEMBER 2011**

**MEMORANDUM**

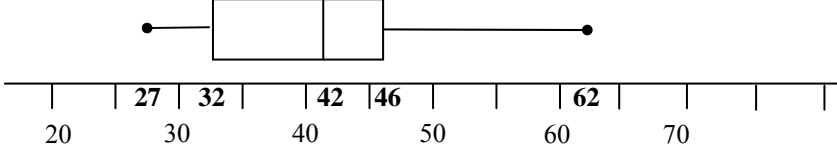
**MARKS: 150**

**This memorandum consists of 22 pages.**

**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum.
- Assuming answers/values in order to solve a problem is not acceptable.

**QUESTION 1**

1.1	Median = 42	✓ answer (1)
1.2	Lower quartile = 32 Upper quartile = 46 Inter quartile range = $46 - 32 = 14$	✓ lower quartile ✓ upper quartile ✓ answer (3)
1.3		✓ box-and-whisker with a median ✓ skewness ✓ indicating <u>5</u> <u>number summary</u> 27; 32; 42; 46; 62 or correct scale (3)
1.4	There is a <b>greater spread</b> of scores to the right of the median (42).  <p style="text-align: center;"><b>OR</b></p> There is a <b>greater spread</b> of scores in the top 50%.  <p style="text-align: center;"><b>OR</b></p> The spread of the scores on the left hand side of the median is closer to each other.  <p style="text-align: center;"><b>OR</b></p> The greatest spread of scores lies between $Q_3$ and the maximum value.  <b>Note:</b> <ul style="list-style-type: none"> <li>• Description about the spread based on the box-and-whisker diagram must be accepted.</li> <li>• If it is indicated that it is skewed to the left because the mean is less than the median: full marks</li> </ul>	✓ greater spread ✓ right of median (42) (2)  ✓ greater spread ✓ top 50% (2)  ✓ spread closer ✓ left of median (2)  ✓ greater spread ✓ between $Q_3$ and max (2)  <p style="text-align: right;"><b>[9]</b></p>

**QUESTION 2**

2.1	$\text{Mean} = \frac{\sum_{i=1}^n x_i}{n} = \frac{580}{8} = 72,5$ <p><b>Note:</b> If rounded off to 73: 1 mark</p>	Answer only: FULL MARKS	✓ 580 ✓ answer (2)
2.2	Standard deviation ( $\sigma$ ) = 2,78 (2,783882181...) <b>Note:</b> If rounded off to 2,8: 1 mark		✓✓ answer (2)
2.3	$\therefore$ 2 golfers' scores lie outside 1 standard deviation of the mean. The interval for 1 standard deviation of the mean is $(72,5 - 2,78 ; 72,5 + 2,78) = (69,72 ; 75,28)$	Answer only: FULL MARKS	✓ interval ✓ number (2) <b>[6]</b>

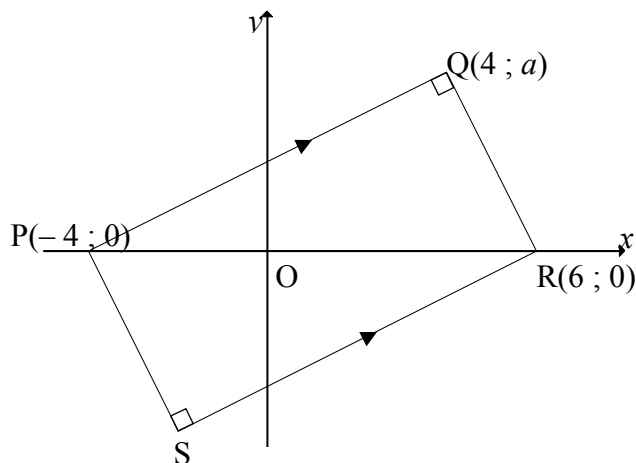
**QUESTION 3**

3.1	30	✓ 30 (1)
3.2	Linear, the points seem to form a straight line.	✓ linear ✓ reason (2)
3.3	The greater the number of hours spent watching TV, the lower the test scores <p style="text-align: center;"><b>OR</b></p> The less time a person spends watching TV, the higher the test score. <p style="text-align: center;"><b>OR</b></p> Negative correlation between the variables <p style="text-align: center;"><b>OR</b></p> Indirect relationship between the variables	✓ deduction (1)
3.4	60 marks. (Accept 50 -70 marks)	✓✓ deduction (2) <b>[6]</b>

**QUESTION 4**

<p>4.1</p>	<table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th>TIME</th> <th>FREQUENCY</th> <th>CUMULATIVE FREQUENCY</th> </tr> </thead> <tbody> <tr> <td><math>1 \leq t &lt; 3</math></td> <td>3</td> <td>3</td> </tr> <tr> <td><math>3 \leq t &lt; 5</math></td> <td>6</td> <td>9</td> </tr> <tr> <td><math>5 \leq t &lt; 7</math></td> <td>7</td> <td>16</td> </tr> <tr> <td><math>7 \leq t &lt; 9</math></td> <td>8</td> <td>24</td> </tr> <tr> <td><math>9 \leq t &lt; 11</math></td> <td>5</td> <td>29</td> </tr> <tr> <td><math>11 \leq t &lt; 13</math></td> <td>1</td> <td>30</td> </tr> </tbody> </table> <p style="text-align: center; border: 1px solid black; padding: 5px;"><b>Note:</b> Only cumulative frequency column – full marks</p>	TIME	FREQUENCY	CUMULATIVE FREQUENCY	$1 \leq t < 3$	3	3	$3 \leq t < 5$	6	9	$5 \leq t < 7$	7	16	$7 \leq t < 9$	8	24	$9 \leq t < 11$	5	29	$11 \leq t < 13$	1	30	<p>One mark for every two correct cumulative frequency values</p> <p style="text-align: right;">(3)</p>
TIME	FREQUENCY	CUMULATIVE FREQUENCY																					
$1 \leq t < 3$	3	3																					
$3 \leq t < 5$	6	9																					
$5 \leq t < 7$	7	16																					
$7 \leq t < 9$	8	24																					
$9 \leq t < 11$	5	29																					
$11 \leq t < 13$	1	30																					
<p>4.2</p>	<p style="text-align: center;"><b>Cumulative Frequency Graph of time taken to answer</b></p>	<ul style="list-style-type: none"> <li>✓ upper limit</li> <li>✓ cumulative frequency (at least 4 of 6 y-values correctly plotted)</li> <li>✓ grounding at (1 ; 0)</li> <li>✓ shape (not joined by a ruler; smooth curve)</li> </ul> <p style="text-align: right;">(4)</p>																					
<p>4.3</p>	<p>Estimated number of learners that took less than 4 minutes: approximately 5 learners (Accept 6) Approximate percentage = 16,67% (Accept 20%)</p> <p><b>Note:</b> If using 9 learners and approximate percentage = 30%: 1 mark If using 5,5 learners and approximate percentage = 18,33%: 1 mark</p>	<ul style="list-style-type: none"> <li>✓ 5 learners</li> <li>✓ 16,67%</li> </ul> <p style="text-align: right;">(2) <b>[9]</b></p>																					

**QUESTION 5**



<p>5.1</p>	$m_{PQ} \times m_{QR} = -1$ $\left(\frac{a-0}{4+4}\right)\left(\frac{a-0}{4-6}\right) = -1$ $\left(\frac{a}{8}\right)\left(\frac{a}{-2}\right) = -1$ $\frac{a^2}{-16} = -1$ $a^2 = 16$ $a = \pm 4$ $a = 4; \text{ since } a > 0$ <p style="text-align: center;"><b>OR</b></p> $PQ^2 + QR^2 = PR^2$ $(8^2 + a^2) + (a^2 + 2^2) = 10^2$ $\therefore 2a^2 = 32$ $\therefore a^2 = 16$ $\therefore a = 4$ <p style="text-align: center;"><b>OR</b></p> <p>Let A be the midpoint of diagonal PR.</p> <p>Then <math>A\left(\frac{-4+6}{2}; \frac{0+0}{2}\right) = A(1; 0)</math>.</p> <p>AQ = AR (diagonals equal and bisect each other)</p> $AQ^2 = AR^2$ $(1-4)^2 + (0-a)^2 = 5^2$ $9 + a^2 = 25$ $a^2 = 16$ $a = 4$ <p><b>Note:</b> If candidate uses <math>a = 4</math> at the beginning, then zero marks.</p>	$\checkmark \frac{a-0}{4+4} \text{ or } \frac{a}{8}$ $\checkmark \frac{a-0}{4-6} \text{ or } \frac{a}{-2}$ <p><math>\checkmark</math> using gradient of perpendicular lines</p> $\checkmark a^2 = 16$ <p style="text-align: right;">(4)</p> <p><math>\checkmark</math> using Pythagoras</p> $\checkmark (8^2 + a^2) + (a^2 + 2^2)$ $\checkmark 10^2$ $\checkmark a^2 = 16$ <p style="text-align: right;">(4)</p> <p><math>\checkmark (1; 0)</math> is centre</p> <p><math>\checkmark AQ = AR</math></p> $\checkmark 3^2 + a^2 = 5^2$ $\checkmark a^2 = 16$ <p style="text-align: right;">(4)</p>
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5.2	<p>Equation of line SR:</p> $m_{PQ} = \frac{4-0}{4-(-4)} = \frac{1}{2}$ $m_{SR} = m_{PQ} = \frac{1}{2} \quad \text{PQ} \parallel \text{SR}$ $y - y_1 = m(x - x_1)$ $y - 0 = \frac{1}{2}(x - 6)$ $y = \frac{1}{2}x - 3$ <p style="text-align: center;"><b>OR</b></p>	<p>✓ <math>m_{PQ} = \frac{1}{2}</math></p> <p>✓ <math>m_{SR} = \frac{1}{2}</math></p> <p>✓ substitution of m and (6 ; 0)</p> <p>✓ standard form (4)</p>
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	$m_{PQ} = \frac{1}{2}$ $m_{PQ} = m_{SR} = \frac{1}{2} \quad \text{PQ} \parallel \text{SR}$ $y = \frac{1}{2}x + c$ $0 = \left(\frac{1}{2}\right)\left(\frac{6}{1}\right) + c$ $-3 = c$ $y = \frac{1}{2}x - 3$ <p style="text-align: center;"><b>OR</b></p> <p>S(-2 ; -4) (translation)</p> $m_{RS} = \frac{0+4}{6+2} = \frac{1}{2}$ $\therefore y + 4 = \frac{1}{2}(x + 2)$ $\therefore y = \frac{1}{2}x - 3$	<p>✓ <math>m_{PQ} = \frac{1}{2}</math></p> <p>✓ <math>m_{SR} = \frac{1}{2}</math></p> <p>✓ substitution of m and (6 ; 0)</p> <p>✓ standard form</p> <p>✓ S(-2 ; -4)</p> <p>✓ <math>m_{SR} = \frac{1}{2}</math></p> <p>✓ substitution of m and (-2 ; -4)</p> <p>✓ standard form (4)</p>
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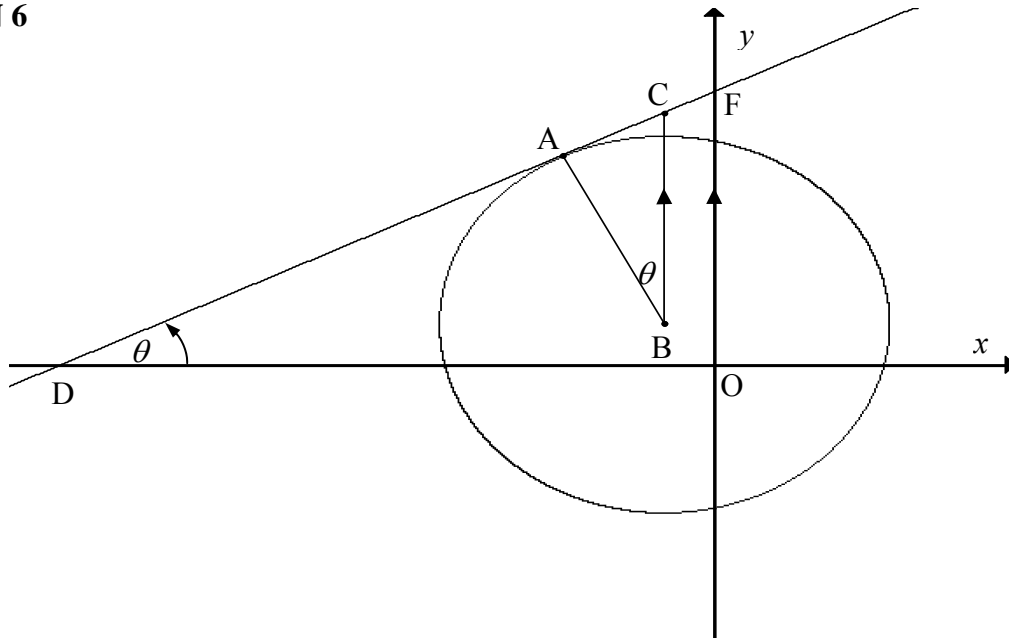
5.3	<p>Eq. of RS: <math>y = \frac{1}{2}x - 3</math></p> <p>Eq. of SP: <math>y - 0 = -2(x + 4)</math></p> $\therefore \frac{1}{2}x - 3 = -2(x + 4)$ $\therefore x = -2$ $y = -4$ <p style="text-align: center;"><b>OR</b></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"> <p>Answer only: FULL MARKS</p> </div>	<p>✓ <math>m = -2</math></p> <p>✓ eq. of SP</p> <p>✓ value of x</p> <p>✓ value of y (4)</p>
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	<p>Midpoint PR = M<math>\left(\frac{-4+6}{2}; \frac{0+0}{2}\right) = (1; 0)</math></p> <p>Let S(x; y). Then since M(1; 0) is this, the midpoint of QS is:</p> $\frac{x_1 + x_2}{2} = 1 \qquad \frac{y_1 + y_2}{2} = 0$ $\therefore \frac{x+4}{2} = 1 \qquad \text{and} \qquad \frac{y+4}{2} = 0$ $x+4 = 2 \qquad y+4 = 0$ $x = -2 \qquad y = -4$ <p style="text-align: center;"><b>OR</b></p> <p>The translation that sends Q(4; 4) to R(6; 0) also sends P(-4; 0) to S.</p> $(6; 0) = (4 + 2; 4 - 4)$ $\therefore S = (-4 + 2; 0 - 4) = (-2; -4)$ <p style="text-align: center;"><b>OR</b></p> <p>The translation that sends Q(4; 4) to P(-4; 0) also sends R(6; 0) to S.</p> $(-4; 0) = (4 - 8; 4 - 4)$ $\therefore S = (6 - 8; 0 - 4) = (-2; -4)$ <p style="text-align: center;"><b>OR</b></p> $m_{PQ} = m_{SR}$ $\frac{1}{2} = \frac{y}{x-6}$ $2y = x - 6 \quad (1)$ $m_{PS} = m_{SR}$ $\frac{y}{x+4} = \frac{4}{-2}$ $-2y = 4x + 16 \quad (2)$ $(1) + (2) : 0 = 5x + 10$ $x = -2$ $\text{Substitute : } 2y = -2 - 6 = -8$ $y = -4$	<p>✓ <math>\frac{x+4}{2} = 1</math></p> <p>✓ <math>\frac{y+4}{2} = 0</math></p> <p>✓ value of x</p> <p>✓ value of y</p> <p style="text-align: right;">(4)</p> <p>✓ method</p> <p>✓ 2 or x + 2</p> <p>✓ -4 or y - 4</p> <p>✓ answer</p> <p style="text-align: right;">(4)</p> <p>✓ method</p> <p>✓ -8 or x - 8</p> <p>✓ -4 or y - 4</p> <p>✓ answer</p> <p style="text-align: right;">(4)</p> <p>✓ equations using the gradient</p> <p>✓ adding the equations</p> <p>✓ value of x</p> <p>✓ value of y</p> <p style="text-align: right;">(4)</p>
<p>5.4</p>	<p>PR = 6 - (-4)</p> <p>= 10</p> <p style="text-align: center;"><b>OR</b></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"> <p>Answer only: FULL MARKS</p> </div> <p>PR<sup>2</sup> = (6+4)<sup>2</sup> + (0-0)<sup>2</sup></p> <p>PR = 10</p>	<p>✓ 6 - (-4)</p> <p>✓ 10</p> <p style="text-align: right;">(2)</p> <p>✓ substitution in correct formula</p> <p>✓ 10</p> <p style="text-align: right;">(2)</p>

<p>5.5</p>	<p>midpoint <math>PR = \left( \frac{6+(-4)}{2}; \frac{0+0}{2} \right) = (1; 0)</math></p> <p>radius of circle <math>= \frac{1}{2} PR = 5</math> units</p> <p><math>\therefore (x-1)^2 + (y-0)^2 = 5^2</math>  <math>(x-1)^2 + y^2 = 25</math></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Answer only: FULL MARKS</p> </div>	<p>✓ midpoint</p> <p>✓ radius</p> <p>✓ eq. of circle in correct form</p> <p style="text-align: right;">(3)</p>
<p>5.6</p>	<p><math>(x-1)^2 + y^2 = 25</math>  substitute <math>Q(4; 4)</math>:  LHS <math>= (4-1)^2 + 4^2</math>  <math>= 25</math>  <math>=</math> RHS  <math>\therefore Q</math> is a point on the circle  <b>Note:</b>  If substitute point into equation resulting in <math>25 = 25</math>: 1 mark  No conclusion: 1 mark</p> <p style="text-align: center;"><b>OR</b></p> <p>Distance from centre <math>(1; 0)</math> to <math>Q(4; 4)</math>  <math>\therefore Q</math> is a point on circle, <math>r = 5</math></p> <p style="text-align: center;"><b>OR</b></p> <p>PR is the diameter of circle PQR therefore Q lies on circle  (<math>P\hat{Q}R = 90^\circ</math>)</p> <p style="text-align: center;"><b>OR</b></p> <p><math>(4-1)^2 + y^2 = 25</math>  <math>y^2 = 16</math>  <math>\therefore y = 4</math>  <math>\therefore Q</math> is a point on the circle</p> <p style="text-align: center;"><b>OR</b></p> <p><math>(x-1)^2 + 4^2 = 25</math>  <math>(x-1)^2 = 9</math>  <math>x-1 = 3</math>  <math>x = 4</math>  <math>\therefore Q</math> is a point on the circle</p>	<p>✓ substitute <math>Q(4;4)</math></p> <p>✓ LHS = RHS</p> <p style="text-align: right;">(2)</p> <p>✓ = 5</p> <p>✓ conclusion</p> <p style="text-align: right;">(2)</p> <p>✓ diameter</p> <p>✓ <math>P\hat{Q}R = 90^\circ</math></p> <p style="text-align: right;">(2)</p> <p>✓ substitute <math>x = 4</math></p> <p>✓ conclusion</p> <p style="text-align: right;">(2)</p> <p>✓ substitute <math>y = 4</math></p> <p>✓ conclusion</p> <p style="text-align: right;">(2)</p>
<p>5.7</p>	<p>P needs to shift at least 4 units to the right and S needs to shift at least 4 units up for the image of PQRS in first quadrant.  <math>\therefore</math> minimum value of <math>k</math> is 4 and minimum value of <math>l</math> is 4  <math>\therefore</math> minimum value of <math>k + l</math> is 8</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p>Answer only: FULL MARKS</p> </div> <p><b>Note:</b> No CA mark applies in 5.7 if <math>k</math> and <math>l</math> are not minimums.</p>	<p>✓ <math>k = 4</math></p> <p>✓ <math>l = 4</math></p> <p>✓ <math>k + l = 8</math></p> <p style="text-align: right;">(3) [22]</p>



**QUESTION 6**



6.1	$x_C = x_B = -1$ $y_C = y_B + 5 = 6$ $\therefore C(-1 ; 6)$	✓ value of $x$ ✓ value of $y$ (2)
6.2	$BA \perp CA$ (tangent $\perp$ radius) $\therefore CA^2 = BC^2 - AB^2$ (Pythagoras) $= (5)^2 - (\sqrt{20})^2 = 5$ $\therefore CA = \sqrt{5}$ or 2,24 units	✓ $BA \perp CA$ or $\hat{BAC} = 90^\circ$ ✓ substitution into Pythagoras ✓ answer (3)
6.3	$\tan \theta = \frac{\sqrt{5}}{\sqrt{20}} = \frac{\sqrt{5}}{2\sqrt{5}} = \frac{1}{2}$	✓ tan ratio ( in any form) (1)
6.4	$m_{DC} \times m_{AB} = -1$ $m_{DC} = \tan \theta = \frac{1}{2}$ $m_{DC} = \frac{1}{2}$ $m_{AB} = -2$	✓ $m_{DC} \times m_{AB} = -1$ ✓ $m_{DC} = \tan \theta = \frac{1}{2}$ (2)

<p>6.5</p>	<p>Eq. of DC: <math>y - 6 = \frac{1}{2}(x + 1)</math>  <math>y = \frac{1}{2}x + \frac{13}{2}</math></p> <p>Eq. of AB: <math>y - 1 = -2(x + 1)</math>  <math>y = -2x - 1</math></p> <p><math>-2x - 1 = \frac{1}{2}x + \frac{13}{2}</math>  <math>-\frac{5}{2}x = \frac{15}{2}</math>  <math>x = -3</math>  <math>y = -2(-3) - 1</math>  <math>y = 5</math>  <math>\therefore A(-3 ; 5)</math></p> <p style="text-align: center;"><b>OR</b></p> <p>Eq. of DC: <math>y - 6 = \frac{1}{2}(x + 1)</math>  <math>y = \frac{1}{2}x + \frac{13}{2}</math></p> <p>Eq. of AB: <math>y - 1 = -2(x + 1)</math>  <math>y = -2x - 1</math></p> <p><u>At A:</u>  <math>x - 2(-2x - 1) + 13 = 0</math>  <math>x + 4x + 2 + 13 = 0</math>  <math>5x = -15</math>  <math>x = -3</math>  and <math>y = -2(-3) - 1 = 5</math>  <math>\therefore A(-3 ; 5)</math></p> <p style="text-align: center;"><b>OR</b></p>	<p>✓ DC: subst <math>m</math> and <math>(-1 ; 6)</math>  ✓ eq. of DC</p> <p>✓ eq. of AB</p> <p>✓ equating equations</p> <p>✓ value of <math>x</math>  ✓ value of <math>y</math> (6)</p> <p>✓ DC: subst <math>m</math> and <math>(-1 ; 6)</math>  ✓ eq. of DC</p> <p>✓ subst <math>m</math> and <math>(-1 ; 1)</math>  ✓ eq. of AB</p> <p>✓ value of <math>x</math>  ✓ value of <math>y</math> (6)</p>
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	<p>Eq. of DC: <math>y - 6 = \frac{1}{2}(x + 1)</math>  <math>y = \frac{1}{2}x + \frac{13}{2}</math></p> <p>Eq. of circle: <math>(x + 1)^2 + (y - 1)^2 = 20</math></p> <p><u>At A:</u>  <math>(x + 1)^2 + (\frac{1}{2}x + \frac{13}{2} - 1)^2 = 20</math>  <math>(x + 1)^2 + (\frac{1}{2}x + \frac{11}{2})^2 = 20</math>  <math>1\frac{1}{4}x^2 + \frac{15}{2}x + 11\frac{1}{4} = 0</math>  <math>\therefore x^2 + 6x + 9 = 0</math>  <math>(x + 3)^2 = 0</math>  <math>\therefore x = -3</math>  and <math>y = \frac{1}{2}(-3) + \frac{13}{2} = 5</math>  <math>\therefore A(-3 ; 5)</math></p>	<p>✓ DC: subst <math>m</math> and <math>(-1 ; 6)</math>  ✓ eq. of DC</p> <p>✓ substitution</p> <p>✓ <math>x^2 + 6x + 9 = 0</math></p> <p>✓ value of <math>x</math>  ✓ value of <math>y</math> (6)</p>
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**OR**

Draw  $AE \perp BC$

$$\cos \theta = \frac{2\sqrt{5}}{5} = \frac{AE}{\sqrt{5}} = \frac{BE}{2\sqrt{5}}$$

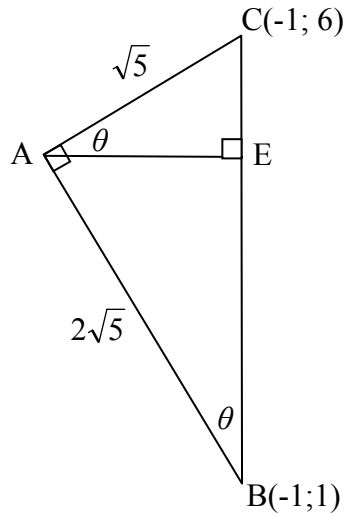
$$\therefore AE = \frac{2 \times 5}{5} = 2$$

$$BE = \frac{4 \times 5}{5} = 4$$

$$x_A = -1 - AE = -1 - 2 = -3$$

$$\therefore y_A = 1 + BE = 4 + 1 = 5$$

$$\therefore A(-3 ; 5)$$



$$\checkmark \frac{2\sqrt{5}}{5} = \frac{AE}{\sqrt{5}}$$

$$\checkmark AE = 2$$

$$\checkmark \frac{2\sqrt{5}}{5} = \frac{BE}{2\sqrt{5}}$$

$$\checkmark BE = 4$$

$$\checkmark -3$$

$$\checkmark 5$$

(6)

**OR**

$$(x+1)^2 + (y-1)^2 = 20 \quad (1)$$

$$y = -2x - 1 \quad (2)$$

$$(x+1)^2 + (-2x-2)^2 = 20$$

$$x^2 + 2x + 1 + 4x^2 + 8x + 4 - 20 = 0$$

$$5x^2 + 10x - 15 = 0$$

$$x^2 + 10x - 15 = 0$$

$$(x+3)(x-1) = 0$$

$$x = -3 \text{ or } x = 1$$

subst (1) in (2)

$$\therefore y = 5$$

✓ subst m and (-1;1)

✓ eq of AB

✓ eq of circle

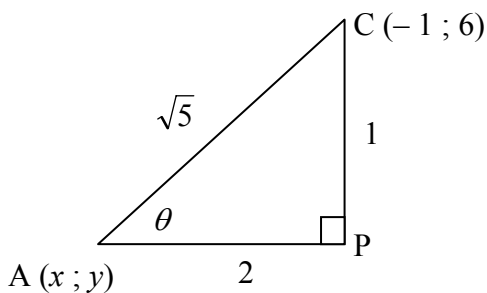
✓ substitution

✓ value of x

✓ value of y (6)

**OR**

Equation AC :  $y = \frac{1}{2}x + 6\frac{1}{2}$



$\tan \theta = \frac{1}{2}$

$\theta = 26,57^\circ$

$AP = \sqrt{5} \cos 26,57^\circ$

$AP = 2$

$CP = \sqrt{5} \sin 26,57^\circ$

$CP = 1$

$\therefore x = -1 - 2 = -3$

$y = 6 - 1 = 5$

$\therefore A(-3; 5)$

✓  $\theta = 26,57^\circ$

✓

$AP = \sqrt{5} \cos 26,57^\circ$

✓  $AP = 2$

✓  $CP = 1$

✓ value of x

✓ value of y

(6)

6.6

Area  $\Delta ABC = \frac{1}{2}(\sqrt{5})(\sqrt{20}) = 5$

Eqn. of DC is  $y = \frac{1}{2}x + \frac{13}{2}$

Therefore  $OF = \frac{13}{2}$  and  $OD = 13$ .

Area  $\Delta ODF = \frac{1}{2}\left(\frac{13}{2}\right)(13) = \frac{169}{4}$

Area  $\Delta ABC$ : Area  $\Delta ODF = 5 : \frac{169}{4} = 20 : 169$

**OR**

$DF^2 = 13^2 + \left(\frac{13}{2}\right)^2 = \frac{845}{4}$

$DF = \frac{13 \cdot \sqrt{5}}{2}$

$$\frac{\Delta_{ABC}}{\Delta_{ODF}} = \frac{\frac{1}{2}(5)(\sqrt{20}) \sin \theta}{\frac{1}{2}(13)\left(\frac{13 \cdot \sqrt{5}}{2}\right) \sin \theta}$$

$$= \frac{20}{169}$$

✓  $\frac{1}{2}(\sqrt{5})(\sqrt{20})$

✓  $OF = \frac{13}{2}$

✓  $OD = 13$

✓  $\frac{1}{2}\left(\frac{13}{2}\right)(13)$

✓ answer

(5)

✓  $= 13^2$

$+ \left(\frac{13}{2}\right)^2 = \frac{845}{4}$

✓  $DF = \frac{13 \cdot \sqrt{5}}{2}$

✓  $\frac{1}{2}(5)(\sqrt{20}) \sin \theta$

✓  $\frac{1}{2}(13)\left(\frac{13 \cdot \sqrt{5}}{2}\right) \sin \theta$

✓ answer (5)

<b>OR</b>	<p><math>\Delta ODF</math> is an enlargement of <math>\Delta ABC</math>  <math>\therefore \text{area } \Delta ABC : \text{area } \Delta ODF = AB^2 : OD^2 = 20 : OD^2</math>                  Equation of DC is <math>y = \frac{1}{2}x + \frac{13}{2}</math>  <math>x_D = -13</math>  <math>OD = 13</math>  <math>\therefore \text{area } \Delta ABC : \text{area } \Delta ODF = AB^2 : OD^2 = 20 : 169</math></p>	<p>✓ enlargement                  ✓✓  <math>AB^2 : OD^2 = 20 : OD^2</math>                  ✓ - 13                  ✓ answer (5)</p> <p style="text-align: right;"><b>[19]</b></p>
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**QUESTION 7**

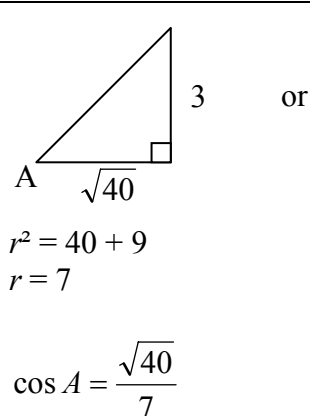
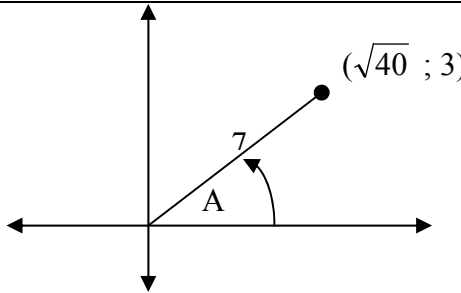
7.1	<p><math>(x; y) \rightarrow (x + 4; y) \rightarrow (-x - 4; -y)</math>                  OR  <math>(x; y) \rightarrow (-x - 4; -y)</math></p>	<p>✓ <math>x + 4</math>                  ✓ <math>y</math>                  ✓ <math>-x - 4</math>                  ✓ <math>-y</math></p> <p style="text-align: right;">(4)</p>
7.2	<p>New centre = <math>(-2; -5)</math>  <math>(x + 2)^2 + (y + 5)^2 = 16</math>  <math>x^2 + 4x + 4 + y^2 + 10y + 25 - 16 = 0</math>  <math>x^2 + y^2 + 4x + 10y + 13 = 0</math></p>	<p>✓ <math>(-2; -5)</math>                  ✓ <math>(x + 2)^2 + (y + 5)^2</math>                  ✓ 16                  ✓ simplification</p> <p style="text-align: right;">(4)</p> <p style="text-align: right;"><b>[8]</b></p>

**QUESTION 8**

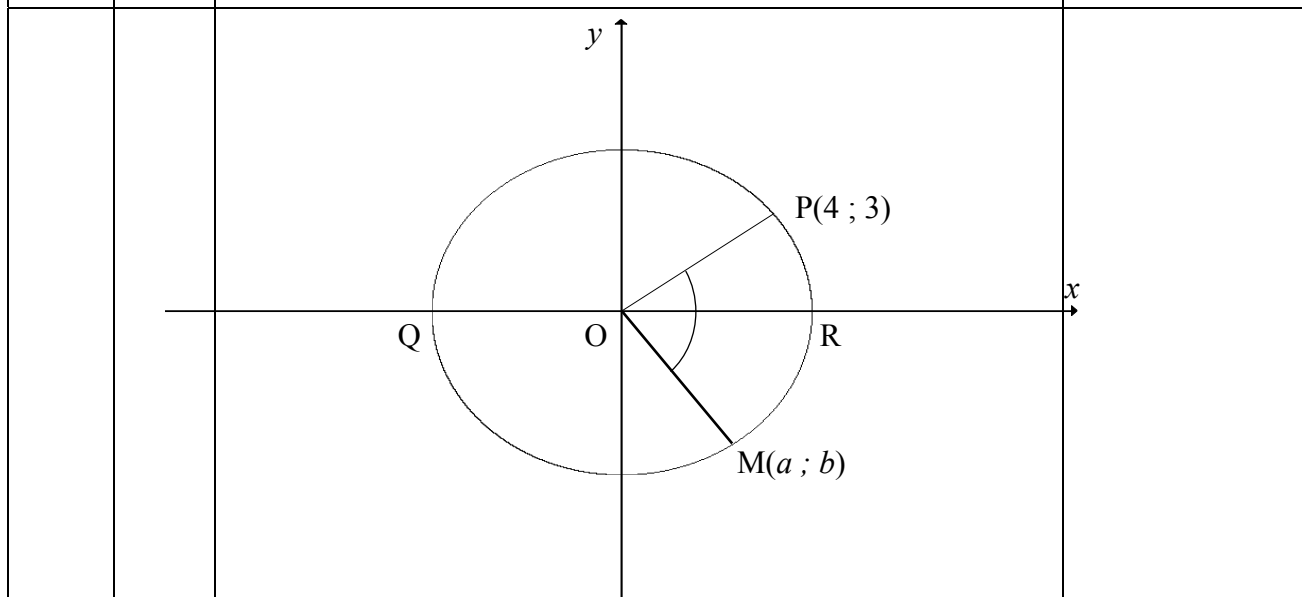
8.1	<p>Rotation of <math>90^\circ</math> anticlockwise about the origin.                  OR                  Rotation of <math>270^\circ</math> clockwise about the origin.  <b>Note:</b> if reflection of <math>90^\circ</math> anticlockwise: 0 marks</p>	<p>✓ rotation <b><math>90^\circ</math></b>                  ✓ anticlockwise (2)                  ✓ rotation <b><math>270^\circ</math></b>                  ✓ clockwise (2)</p>
8.2	<p>D(5 ; -4)  <math>D'(4 ; 5)</math></p>	<p>✓ 4                  ✓ 5</p> <p style="text-align: right;">(2)</p>
8.3	<p>G (-7 ; -6)</p>	<p>✓ -7                  ✓ -6</p> <p style="text-align: right;">(2)</p>
8.4	<p>Area ABCD = <math>5 \times 2 = 10</math> square units                  Area MNRP = <math>10 \times \left(\frac{3}{2}\right)^2 = \frac{45}{2}</math>                  Area ABCD <math>\times</math> Area MNRP  <math>= 10 \times \frac{9}{4} \times 10</math>  <math>= 225 \text{ (units)}^4</math></p> <p style="text-align: center;"><b>OR</b></p>	<p>✓ area ABCD = 10                  ✓ area MNRP  <math>= \frac{45}{2}</math>                  ✓ 225</p> <p style="text-align: right;">(3)</p>

	$\text{Product} = \left(\frac{3}{2}\right)^2 \times (\text{area ABCD})^2$ $= \frac{9}{4} \times (5 \times 2)^2$ $= 225 (\text{units})^4$ <p>Note: CA will apply if <math>\left(\frac{3}{2}\right)^2</math> used in calculation.</p>	<p>✓ <math>\left(\frac{3}{2}\right)^2</math></p> <p>✓ <math>10^2</math></p> <p>✓ 225</p> <p style="text-align: right;">(3) <b>[9]</b></p>
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**QUESTION 9**

9.1	9.1.1	 <p style="text-align: center;">or</p> 	<p>✓ sketch</p> <p>✓ <math>r = 7</math></p> <p>✓ <math>\frac{\sqrt{40}}{7}</math></p> <p style="text-align: right;">(3)</p>
	9.1.2	$\sin(180^\circ + A)$ $= -\sin A$ $= -\frac{3}{7}$ <p style="text-align: center;"><b>OR</b></p> $\sin(180^\circ + A) = \sin 180^\circ \cdot \cos A + \cos 180^\circ \cdot \sin A$ $= 0 \cdot \cos A - 1 \cdot \sin A$ $= -\sin A$ $= -\frac{3}{7}$	<p>✓ <math>-\sin A</math></p> <p>✓ <math>-\frac{3}{7}</math></p> <p style="text-align: right;">(2)</p> <p>✓ <math>-\sin A</math></p> <p>✓ <math>-\frac{3}{7}</math></p> <p style="text-align: right;">(2)</p>
9.2		$\frac{\cos 100^\circ \times \tan^2 120^\circ}{\sin(-10^\circ)}$ $= \frac{(-\cos 80^\circ)(-\tan 60^\circ)^2}{(-\sin 10^\circ)}$ $= \frac{(-\cos 80^\circ) \times ((-\sqrt{3})^2)}{(-\cos 80^\circ)}$ $= 3$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> Answer only: 0 marks</p> </div> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> If <math>\frac{+\cos 80^\circ}{+\sin 10^\circ}</math> (assume two negatives cancelled), no penalty</p> </div>	<p>✓ <math>-\cos 80^\circ</math></p> <p>✓ <math>-\tan 60^\circ</math> or <math>\tan^2 60^\circ</math></p> <p>✓ <math>-\sin 10^\circ</math></p> <p>✓ <math>-\sqrt{3}</math></p> <p>✓ <math>\sin 10^\circ = \cos 80^\circ</math></p> <p>✓ 3</p> <p style="text-align: right;">(6)</p>

		<p style="text-align: center;"><b>OR</b></p> $\frac{\cos 100^\circ \times \tan^2 120^\circ}{\sin(-10^\circ)}$ $= \frac{(-\cos 80^\circ)(-\tan 60^\circ)^2}{(-\sin 10^\circ)}$ $= \frac{(-\sin 10^\circ) \times ((-\sqrt{3})^2)}{(-\sin 10^\circ)}$ $= 3$ <p style="text-align: center;"><b>OR</b></p> $\frac{\cos 100^\circ}{\sin(-10^\circ)} \times \tan^2 120^\circ$ $= \frac{\cos(90^\circ + 10^\circ)}{-\sin(10^\circ)} \times \tan^2 60^\circ$ $= \frac{-\sin 10^\circ}{-\sin 10^\circ} \times (\sqrt{3})^2$ $= 3$	<ul style="list-style-type: none"> <li>✓ <math>-\cos 80^\circ</math></li> <li>✓ <math>-\sin 10^\circ</math></li> <li>✓ <math>-\tan 60^\circ</math></li> <li>✓ <math>-\sqrt{3}</math></li> <li>✓ <math>\cos 80^\circ = \sin 10^\circ</math></li> <li>✓ 3</li> </ul> <p style="text-align: right;">(6)</p>
		$\frac{\cos 100^\circ}{\sin(-10^\circ)} \times \tan^2 120^\circ$ $= \frac{\cos(90^\circ + 10^\circ)}{-\sin(10^\circ)} \times \tan^2 60^\circ$ $= \frac{-\sin 10^\circ}{-\sin 10^\circ} \times (\sqrt{3})^2$ $= 3$	<ul style="list-style-type: none"> <li>✓ <math>\cos(90^\circ + 10^\circ)</math></li> <li>✓ <math>-\sin 10^\circ</math></li> <li>✓ <math>-\sin 10^\circ</math></li> <li>✓ <math>\tan^2 60^\circ</math></li> <li>✓ <math>\sqrt{3}</math></li> <li>✓ 3</li> </ul> <p style="text-align: right;">(6)</p>



9.3	9.3.1	$r = 5$ $\sin \hat{R}OP = \frac{3}{5} = 0,6$	<ul style="list-style-type: none"> <li>✓ 5</li> <li>✓ ratio</li> </ul> <p style="text-align: right;">(2)</p>
	9.3.2	$\hat{R}OP = 36,87^\circ$ $\hat{Q}OP = 180^\circ - 36,869\dots^\circ$ $\hat{Q}OP = 143,13^\circ$	<div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;">                 Answer only: Full Marks             </div> <ul style="list-style-type: none"> <li>✓ <math>36,869\dots^\circ</math></li> <li>✓ <math>143,13^\circ</math></li> </ul> <p style="text-align: right;">(2)</p>

<p>9.3.3</p>	$x_m = x \cos \theta + y \sin \theta$ $a = 4 \cos 115^\circ + 3 \sin 115^\circ$ $a = 1,03$	<div style="border: 1px solid black; padding: 5px;"> <p><b>Note:</b> Penalise 1 mark for rounding incorrectly <b>Note:</b> If incorrect angle is used in the x- formula: 1 mark</p> </div> <p style="text-align: center;"><b>OR</b></p> <p>Rotation of <math>115^\circ</math> clockwise = <math>245^\circ</math> anticlockwise</p> $x_m = x \cos \theta - y \sin \theta$ $a = 4 \cos 245^\circ - 3 \sin 245^\circ$ $a = 1,03$ <p style="text-align: center;"><b>OR</b></p> $\tan \hat{P\hat{O}R} = \frac{3}{4}$ $\hat{P\hat{O}R} = 36,86\dots^\circ$ $\hat{M\hat{O}R} = 78,13\dots^\circ$ $\cos \hat{M\hat{O}R} = \frac{a}{5}$ $a = 5 \cos 78,13^\circ$ $a = 1,03$	<p>✓ formula ✓ substitution of values ✓ <math>a = 1,03</math> (3)</p> <p>✓ formula ✓ substitution of values ✓ <math>a = 1,03</math> (3)</p> <p>✓ <math>36,86^\circ</math></p> <p>✓ cos ratio</p> <p>✓ <math>a = 1,03</math> (3)</p> <p style="text-align: right;"><b>[18]</b></p>
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**QUESTION 10**

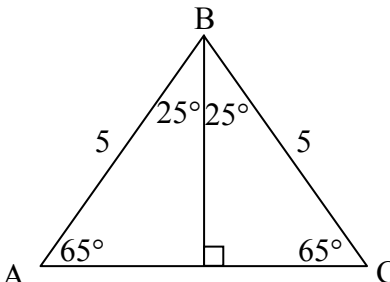
<p>10.1</p>	$f(225^\circ) = 2$ $\therefore a \tan 225^\circ = 2 \quad \therefore a = 2$ $g(0) = 4$ $\therefore b \cos 0^\circ = 4 \quad \therefore b = 4$	<div style="border: 1px solid black; padding: 5px; text-align: center;"> <p>Answer only: Full marks</p> </div>	<p>✓ substitution ✓ <math>a = 2</math></p> <p>✓ substitution ✓ <math>b = 4</math> (4)</p>
<p>10.2</p>	<p>Minimum value of <math>g(x) + 2 = -4 + 2 = -2</math></p>	<div style="border: 1px solid black; padding: 5px; text-align: center;"> <p>Answer only: Full marks</p> </div>	<p>✓ <math>-4</math> ✓ <math>-2</math> (2)</p>
<p>10.3</p>	$\text{Period} = \frac{180^\circ}{\frac{1}{2}} = 360^\circ$	<div style="border: 1px solid black; padding: 5px; text-align: center;"> <p>Answer only: Full marks</p> </div>	<p>✓ <math>\frac{180^\circ}{\frac{1}{2}}</math> ✓ <math>360^\circ</math> (2)</p>



10.4	<p>At P <math>f(\theta) = g(\theta)</math>  <math>2 \tan \theta = 4 \cos \theta</math>                  for <math>180^\circ - \theta</math>: <math>2 \tan (180^\circ - \theta) = -2 \tan \theta</math>                  and <math>4 \cos(180^\circ - \theta) = -4 \cos \theta</math>  <math>2 \tan \theta = 4 \cos \theta</math> at P  <math>\therefore -2 \tan \theta = -4 \cos \theta</math>  <math>\therefore 2 \tan (180^\circ - \theta) = 4 \cos (180^\circ - \theta)</math> at Q</p> <p style="text-align: center;"><b>OR</b></p> <p><math>2 \tan \theta = 4 \cos \theta</math>  <math>\frac{\sin \theta}{\cos \theta} = 2 \cos \theta</math>  <math>\sin \theta = 2 \cos^2 \theta</math>  <math>= 2(1 - \sin^2 \theta)</math>  <math>2 \sin^2 \theta + \sin \theta - 2 = 0</math>  <math>\sin \theta = \frac{-1 \pm \sqrt{1 - 4(2)(-2)}}{4}</math>  <math>\sin \theta = 0,78077\dots</math>  <math>\theta = 51,33^\circ</math> or <math>128,67^\circ</math>  <math>\therefore</math> the x - coordinate of Q is <math>180^\circ - x_p</math></p>	<p><math>\checkmark 2 \tan \theta = 4 \cos \theta</math>  <math>\checkmark 2 \tan (180^\circ - \theta) = -2 \tan \theta</math>  <math>\checkmark 4 \cos(180^\circ - \theta) = -4 \cos \theta</math>  <math>\checkmark 2 \tan (180^\circ - \theta) = 4 \cos (180^\circ - \theta)</math> (4)</p> <p><math>\checkmark</math> equation</p> <p><math>\checkmark \sin \theta = 0,78077\dots</math>  <math>\checkmark 51,33^\circ</math>  <math>\checkmark 128,67^\circ</math> (4)</p> <p style="text-align: right;"><b>[12]</b></p>
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**QUESTION 11**

11.1	<p>Area <math>\Delta ABC = \frac{1}{2} \cdot AB \cdot BC \cdot \sin 50^\circ</math>  <math>= \frac{1}{2} (5)(5) \sin 50^\circ</math>  <math>= 9,58 \text{ units}^2</math></p> <p style="text-align: center;"><b>OR</b></p> <p>Area of <math>\Delta ABC</math>  <math>= \frac{1}{2} (2)(5) \sin 25^\circ (5 \cos 25^\circ)</math>  <math>= 9,58 \text{ units}^2</math></p> <div style="text-align: center;"> <p>The diagram shows an isosceles triangle ABC with AB = BC = 5. The base angles are 65 degrees and the vertex angle is 50 degrees. A vertical line from B to the base AC is perpendicular to AC, forming two right-angled triangles with angles 25 degrees and 65 degrees.</p> </div> <p style="text-align: center;"><b>OR</b></p> <p>Area of <math>\Delta ABC</math>  <math>= [\frac{1}{2} (5 \cos 65^\circ)(5 \sin 65^\circ)](2)</math>  <math>= 9,58 \text{ units}^2</math></p>	<p><math>\checkmark</math> substitution into correct formula</p> <p><math>\checkmark</math> answer (2)</p> <p><math>\checkmark</math> base and height in terms of 5 and <math>25^\circ</math>  <math>\checkmark</math> answer (2)</p> <p><math>\checkmark</math> base and height in terms of 5 and <math>65^\circ</math>  <math>\checkmark</math> answer (2)</p>
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<p>11.2</p>	<p> <math>AC^2 = 5^2 + 5^2 - 2(5)(5) \cos 50^\circ</math>  <math>AC^2 = 17,86061952</math>  <math>AC = 4,23 \text{ units}</math> </p> <p style="text-align: center;"><b>OR</b></p> <p> <math>\hat{A} = \hat{C} = 65^\circ</math> (angles opposite equal sides)  <math>\frac{\sin 65^\circ}{5} = \frac{\sin 50^\circ}{AC}</math>  <math>AC = \frac{5 \sin 50^\circ}{\sin 65^\circ}</math>  <math>= 4,23 \text{ units}</math> </p> <p style="text-align: center;"><b>OR</b></p> <p> <math>\sin 25^\circ = \frac{\frac{1}{2}(AC)}{5}</math>  <math>AC = 2(5) \sin 25^\circ</math>  <math>= 4,23 \text{ units}</math> </p> <div style="text-align: center;">  </div> <p style="text-align: center;"><b>OR</b></p> <p> <math>\cos 65^\circ = \frac{\frac{1}{2}(AC)}{5}</math>  <math>AC = 2(5) \cos 65^\circ</math>  <math>AC = 4,23 \text{ units}</math> </p>	<p>                 ✓ use of cosine rule                  ✓ substitution                  ✓ answer (3)             </p> <p>                 ✓ use of sine rule                  ✓ substitution                  ✓ answer (3)             </p> <p>                 ✓ sketch/diagram                  ✓ <math>\sin 25^\circ = \frac{\frac{1}{2}AC}{5}</math>                  ✓ answer (3)             </p> <p>                 ✓ sketch/diagram                  ✓ <math>\cos 65^\circ = \frac{\frac{1}{2}(AC)}{5}</math>                  ✓ answer (3)             </p>
<p>11.3</p>	<p> <math>\tan 25^\circ = \frac{CF}{AC}</math>  <math>\therefore CF = 4,23 \times \tan 25^\circ</math>  <math>\therefore CF = 1,97 \text{ units}</math> </p> <p style="text-align: center;"><b>OR</b></p> <p> <math>\frac{FC}{\sin 25^\circ} = \frac{4,23}{\sin 65^\circ}</math>  <math>FC = \frac{4,23 \sin 25^\circ}{\sin 65^\circ}</math>  <math>= 1,97 \text{ units}</math> </p>	<p>                 ✓ ratio                  ✓ CF as subject                  ✓ answer (3)             </p> <p>                 ✓ sine rule                  ✓ FC as subject                  ✓ answer (3)             </p> <p style="text-align: right;"><b>[8]</b></p>

**QUESTION 12**

<p>12.1</p>	$LHS = \frac{\sin(360^\circ + 90^\circ + x - \alpha)}{\cos(\alpha - x)}$ $= \frac{\sin(90^\circ + x - \alpha)}{\cos(\alpha - x)}$ $= \frac{\cos(x - \alpha)}{\cos(\alpha - x)}$ $= \frac{\cos(\alpha - x)}{\cos(\alpha - x)}$ $= 1$ <p style="text-align: center;"><b>OR</b></p> $LHS = \frac{\sin[90^\circ - (\alpha - x)]}{\cos(\alpha - x)}$ $= \frac{\cos(\alpha - x)}{\cos(\alpha - x)}$ $= 1$ $= RHS$	<p>✓ subtracting 360° ✓ cos (x - α)</p> <p>✓ cos(α - x)</p> <p style="text-align: right;">(3)</p> <p>✓ subtracting 360° ✓ writing as 90° - (α - x) ✓ cos(α - x)</p> <p style="text-align: right;">(3)</p>
<p>12.2</p>	$\cos 2x = 1 - 3 \cos x$ $2 \cos^2 x - 1 = 1 - 3 \cos x$ $2 \cos^2 x + 3 \cos x - 2 = 0$ $(2 \cos x - 1)(\cos x + 2) = 0$ $\cos x = \frac{1}{2} \quad \text{or} \quad \cos x = -2$ <p style="text-align: center;">n/a</p> $x = 60^\circ + k.360^\circ ; k \in \mathbb{Z} \quad \text{or} \quad x = 300^\circ + k.360^\circ ; k \in \mathbb{Z}$ <p style="text-align: center;"><b>OR</b></p> $x = \pm 60^\circ + k.360^\circ ; k \in \mathbb{Z}$	<p>✓ cos 2x = 2 cos<sup>2</sup> x - 1</p> <p>✓ factorisation ✓ cos x = <math>\frac{1}{2}</math></p> <p>✓ 60° ✓ 300° ✓ + k.360° ✓ k ∈ Z</p> <p style="text-align: right;">(7)</p>
<p>12.3.1</p>	<p>LHS:</p> $\frac{\sin A \cos B - \cos A \sin B}{\sin B \cos B}$ $= \frac{\sin(A - B)}{\sin B \cos B}$ <p>RHS = <math>\frac{2 \sin(A - B)}{2 \sin B \cos B}</math></p> $= \frac{\sin(A - B)}{\sin B \cos B}$ $= LHS$	<p>✓ writing as single fraction ✓ comp. angle expansion ✓ comp. angle expansion ✓ simplification</p> <p style="text-align: right;">(4)</p>

	<p><b>OR</b></p> <p>LHS:</p> $\frac{\sin A \cos B - \cos A \sin B}{\sin B \cos B}$ $= \frac{\sin(A - B)}{\sin B \cos B}$ $= \frac{2 \sin(A - B)}{2 \sin B \cos B}$ $= \frac{2 \sin(A - B)}{\sin 2B}$ $= RHS$	<p>✓ writing as single fraction                  ✓ comp. angle expansion                  ✓ mult. by 2                  ✓ comp. angle expansion</p> <p style="text-align: right;">(4)</p>
	<p><b>OR</b></p> <p>RHS = <math>\frac{2 \sin(A - B)}{\sin 2B}</math></p> $= \frac{2(\sin A \cos B - \cos A \sin B)}{2 \sin B \cos B}$ $= \frac{\sin A \cos B - \cos A \sin B}{\sin B \cos B}$ $= \frac{\sin A \cos B}{\sin B \cos B} - \frac{\cos A \sin B}{\sin B \cos B}$ $= \frac{\sin A}{\sin B} - \frac{\cos A}{\cos B}$ $= LHS$	<p>✓ expansion                  ✓ expansion                  ✓ divide by 2                  ✓ write as separate fractions</p> <p style="text-align: right;">(4)</p>

<p>12.3.2(a)</p>	$\begin{aligned} A = 5B \\ \frac{\sin 5B}{\sin B} - \frac{\cos 5B}{\cos B} &= \frac{2 \sin(5B - B)}{\sin 2B} \\ &= \frac{2 \sin 4B}{\sin 2B} \\ &= \frac{4 \sin 2B \cos 2B}{\sin 2B} \\ &= 4 \cos 2B \end{aligned}$ <p style="text-align: center;"><b>OR</b></p> $\begin{aligned} \frac{\sin 5B}{\sin B} - \frac{\cos 5B}{\cos B} \\ &= \frac{\sin 5B \cos B - \cos 5B \sin B}{\sin B \cos B} \\ &= \frac{\sin(5B - B)}{\sin B \cos B} \\ &= \frac{\sin 4B}{\sin B \cos B} \\ &= \frac{1}{2} (2) \sin B \cos B \\ &= \frac{2 \sin 2B \cos 2B}{\frac{1}{2} \sin 2B} \\ &= 4 \cos 2B \end{aligned}$	<p>✓ recognising A = 5B ✓ substituting A = 5B ✓ sin 4B = 2 sin 2B cos 2B</p> <p style="text-align: right;">(3)</p> <p>✓ writing as single fraction</p> <p>✓ sin 4B = 2 sin 2B cos 2B</p> <p>✓ compound angle in denominator</p> <p style="text-align: right;">(3)</p>
<p>12.3.2(b)</p>	$\begin{aligned} B = 18^\circ \\ \frac{\sin 90^\circ}{\sin 18^\circ} - \frac{\cos 90^\circ}{\cos 18^\circ} &= 4 \cos 2(18^\circ) \\ \therefore \frac{1}{\sin 18^\circ} - 0 &= 4 \cos 36^\circ \\ \therefore \frac{1}{\sin 18^\circ} &= 4 \cos 36^\circ \end{aligned}$	<p>✓ recognising B = 18° ✓ substituting B = 18° ✓ simplify</p> <p style="text-align: right;">(3)</p>
<p>12.3.2(c)</p>	<p>Let <math>\sin 18^\circ = a</math></p> $\begin{aligned} \frac{1}{\sin 18^\circ} &= 4 \cos 36^\circ \\ \frac{1}{\sin 18^\circ} &= 4(1 - 2 \sin^2 18^\circ) \\ \therefore \frac{1}{a} &= 4(1 - 2a^2) \\ \therefore 1 &= 4a - 8a^3 \\ \therefore 8a^3 - 4a + 1 &= 0 \end{aligned}$ <p>Hence <math>\sin 18^\circ</math> is a solution of <math>\therefore 8x^3 - 4x + 1 = 0</math></p> <p style="text-align: center;"><b>OR</b></p>	<p>✓ <math>\sin 18^\circ = a</math> ✓ <math>\cos 36^\circ</math> = <math>1 - 2 \sin^2 18^\circ</math> ✓ substitution of <math>a</math> ✓ simplification</p> <p style="text-align: right;">(4)</p>

	$\frac{1}{\sin 18^\circ} = 4 \cos 36^\circ$ $\frac{1}{\sin 18^\circ} = 4(1 - 2 \sin^2 18^\circ)$ $\frac{1}{\sin 18^\circ} = 4 - 8 \sin^2 18^\circ$ $8(\sin 18^\circ)^3 - 4(\sin 18^\circ) + 1 = 0$ <p>Hence <math>\sin 18^\circ</math> is a solution of <math>\therefore 8x^3 - 4x + 1 = 0</math></p> <p><b>Note:</b> substituting <math>x = \sin 18^\circ</math> into <math>8x^3 - 4x + 1</math> using a calculator showing equal to 0: 0 marks</p>	<p>✓ <math>\cos 36^\circ</math>  <math>= 1 - 2 \sin^2 18^\circ</math>  ✓ simplification  ✓ equation i.t.o  <math>\sin 18^\circ</math>  ✓ replacing  <math>\sin 18^\circ = x</math></p> <p style="text-align: right;">(4) [24]</p>
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**TOTAL: 150**